

Section 10

$$\begin{aligned} \textcircled{7} \quad f(x) &= \cos x & f(-4\pi/3) &= -1/2 \\ f'(x) &= -\sin x & f'(-4\pi/3) &= +\sqrt{3}/2 \\ f''(x) &= -\cos x & f''(-4\pi/3) &= +1/2 \\ f'''(x) &= +\sin x & f'''(-4\pi/3) &= -\sqrt{3}/2 \end{aligned}$$

$$-\frac{1}{2} + \frac{\sqrt{3}}{2}(x + 4\pi/3) + \frac{1}{2} \cdot \frac{1}{2} (x + 4\pi/3)^2 - \frac{\sqrt{3}}{2} \cdot \frac{1}{3!} (x + \frac{4\pi}{3})^3 + \dots$$

$$\begin{aligned} \textcircled{8} \quad f(x) &= e^x & f(e) &= e^e \\ f'(x) &= e^x & f'(e) &= e^e \\ f''(x) &= e^x & f''(e) &= e^e \end{aligned}$$

$$e^e + e^e(x-e) + \frac{e^e}{2!}(x-e)^2 + \frac{e^e}{3!}(x-e)^3 + \dots$$

$$\boxed{\sum_{n=0}^{\infty} \frac{e^e (x-e)^n}{n!}} \quad \checkmark$$

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$$f(x) = xe^x$$

$$\sum_{n=0}^{\infty} \frac{x^{n+1}}{n!}$$

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$$f(x) = x^{1/3}$$

$$x = 8$$

$$f'(x) = \frac{1}{3} x^{-2/3}$$

$$f(8) = 2$$

$$f'(8) = \frac{1}{3 \cdot 4} = \frac{1}{12}$$

5/12

